

LLN_UniformSq.m

```
function [n,RunningAve,TrueMean] = LLN_UniformSq(N)

% function [n,RunningAve,TrueMean] = LLN_UniformSq(N)
%
% The Law of Large Numbers for the squared uniform distribution.
%
% Choose N i.i.d. random variables from the distribution of  $U^2$ ,
% where  $U$  is the uniform distribution on the interval  $[0,1]$ .
% For each  $n = 1:N$ , compute the running average of the first  $n$ 
% random variables. Also, for each  $n$  record the true mean
% (which is  $1/3$ ) so that the results can be easily plotted with
% plot(n,RunningAve,n,TrueMean).

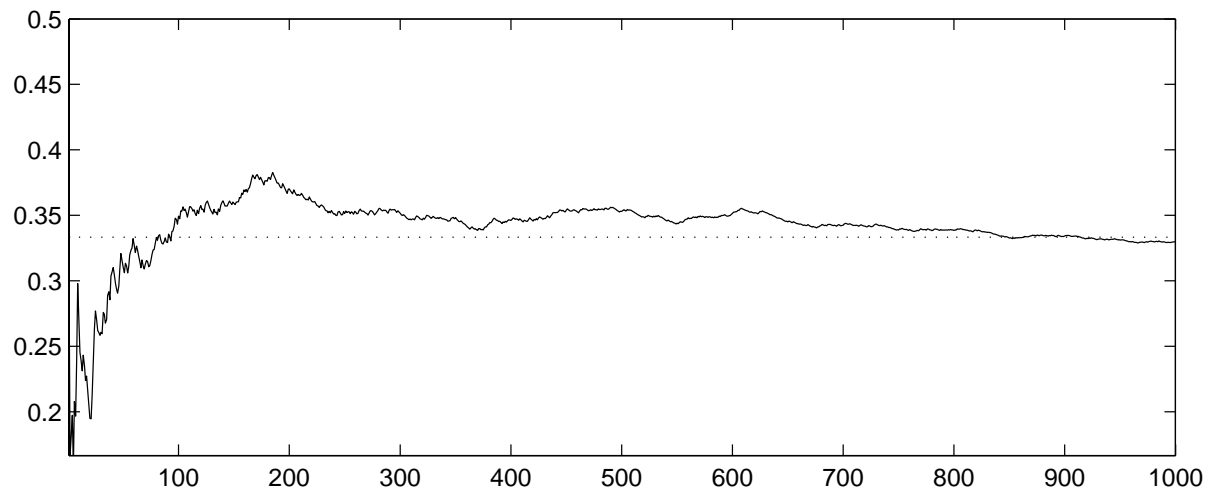
RunningSum = 0;           % initialize the sum of the random variables
for k = 1:N

    Usq = rand^2; % rand returns (approximately) a sample from the uniform
                  % distribution on  $[0,1]$ . Successive calls to rand give
                  % (approximately) independent samples. So Usq are
                  % i.i.d. samples from squared uniform distribution.

    RunningSum = RunningSum + Usq;
    RunningAve(k) = RunningSum / k;
    TrueMean(k) = 1/3;
end

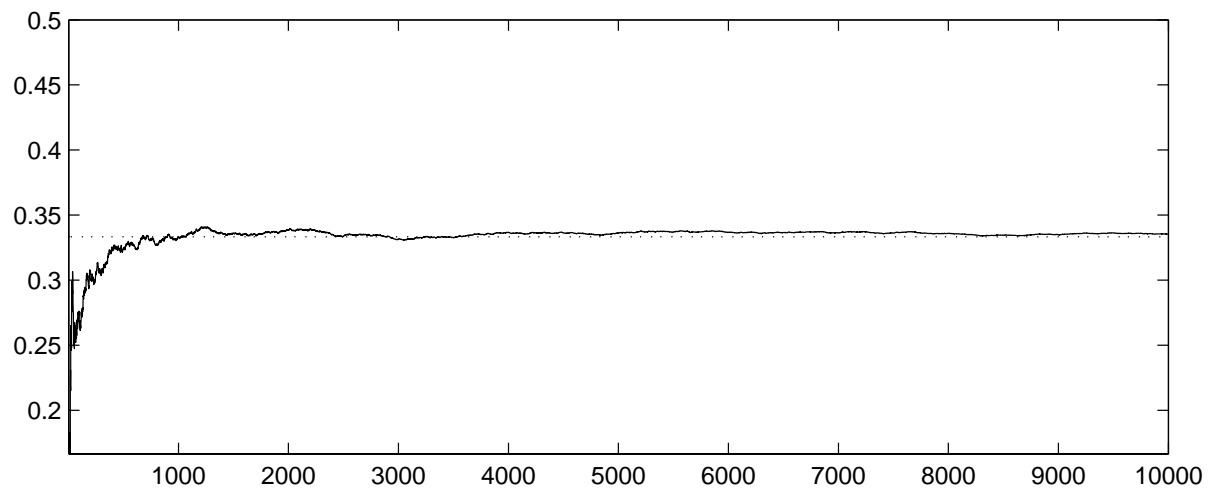
n = [1:N];

return
```



The above figure was made with the following commands:

```
[n,RunningAve,TrueMean] = LLN_UniformSq(1000);
plot(n,RunningAve,'-',n,TrueMean,':')
axis([1 1000 1/6 3/6])
```



The above figure was made with the following commands:

```
[n,RunningAve,TrueMean] = LLN_UniformSq(10000);
plot(n,RunningAve,'-',n,TrueMean,':')
axis([1 10000 1/6 3/6])
```