Linear Algebra

MA 242 (Spring 2013) Instructor: M. Chirilus-Bruckner

INVERTIBLE MATRICES

- some rules and facts -

1. If A is an invertible $n \times n$ matrix, then for each $b \in \mathbb{R}^n$, the equation Ax = b has a unique solution $x = A^{-1}b$.

Why?

2. If A is an invertible matrix, then A^{-1} is invertible and

$$(A^{-1})^{-1} = A.$$

Why?

3. If A and B are invertible matrices, then so is AB with inverse

$$(AB)^{-1} = B^{-1}A^{-1}.$$

Why?

4. If A is an invertible matrix, then so is A^T with inverse

$$\left(A^{T}\right)^{-1} = \left(A^{-1}\right)^{T}.$$

Why?