

Title: *Lagrangian Dynamics on an infinite-dimensional torus.*

Abstract: The space $L^2(0, 1)$ has a natural Riemannian structure on the basis of which we introduce an $L^2(0, 1)$ -infinite dimensional torus \mathbb{T} . We consider the group \mathcal{G} of bijections $G : [0, 1] \rightarrow [0, 1]$ which preserve Lebesgue measure. We also consider a class of Hamiltonians defined on the cotangent bundle of \mathbb{T} , invariant under the action of \mathcal{G} . We establish existence of a viscosity solution for a *cell problem* on \mathbb{T} , that are invariant under the action of \mathcal{G} . We apply this to the study of one-dimensional nonlinear Vlasov system with periodic potential. (This is a joint work with A. Tudorascu).