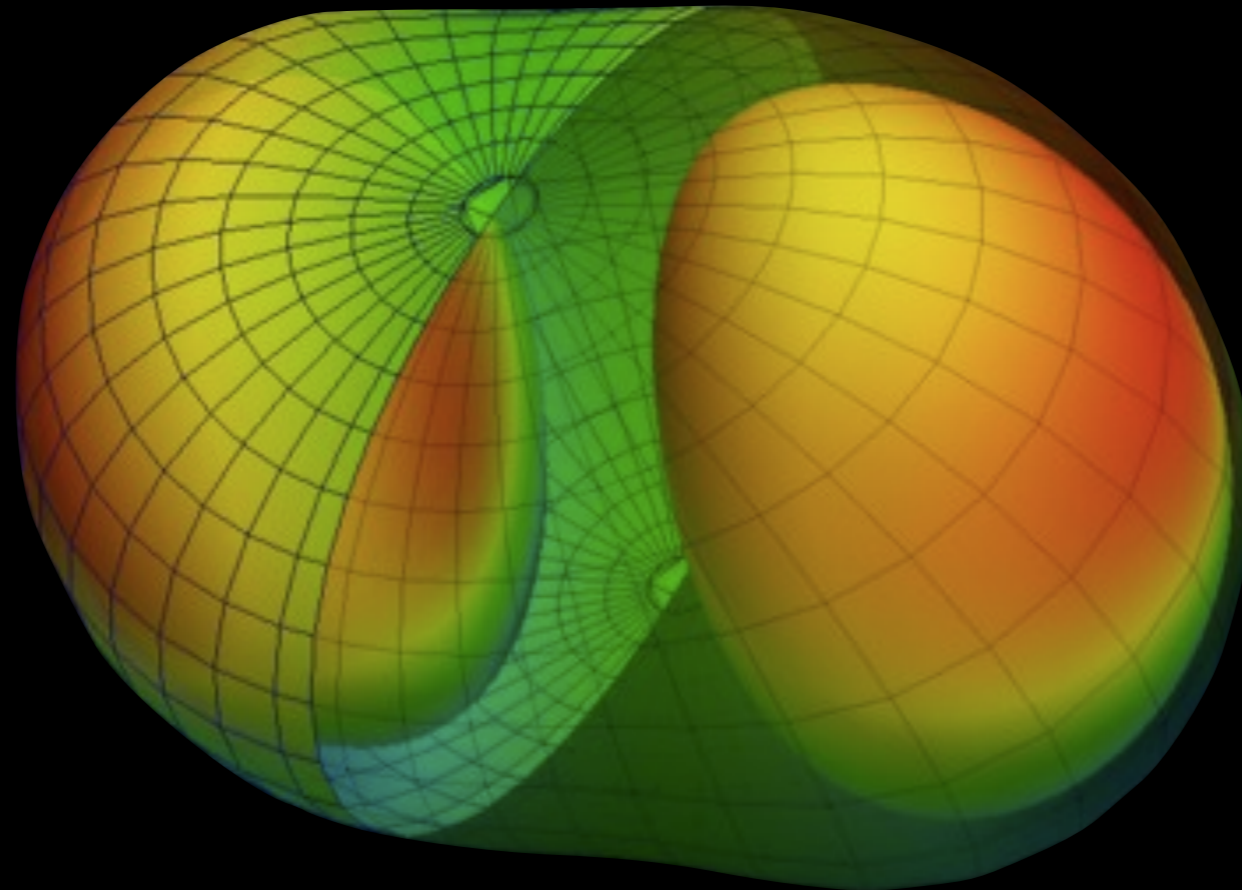


Simulating merging black holes with spins beyond the Bowen-York limit



Geoffrey Lovelace (Cornell)

in collaboration with

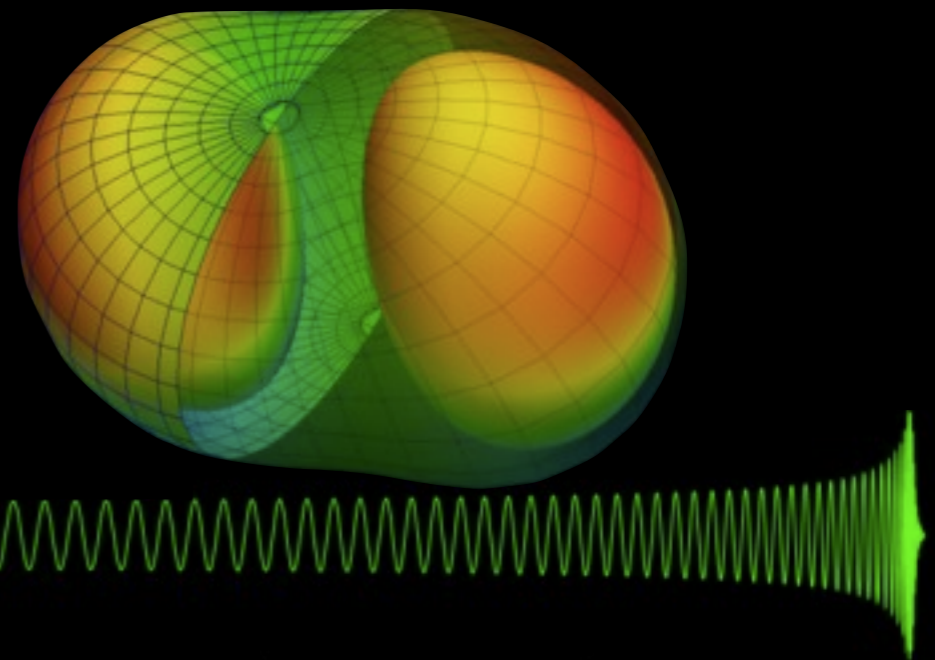
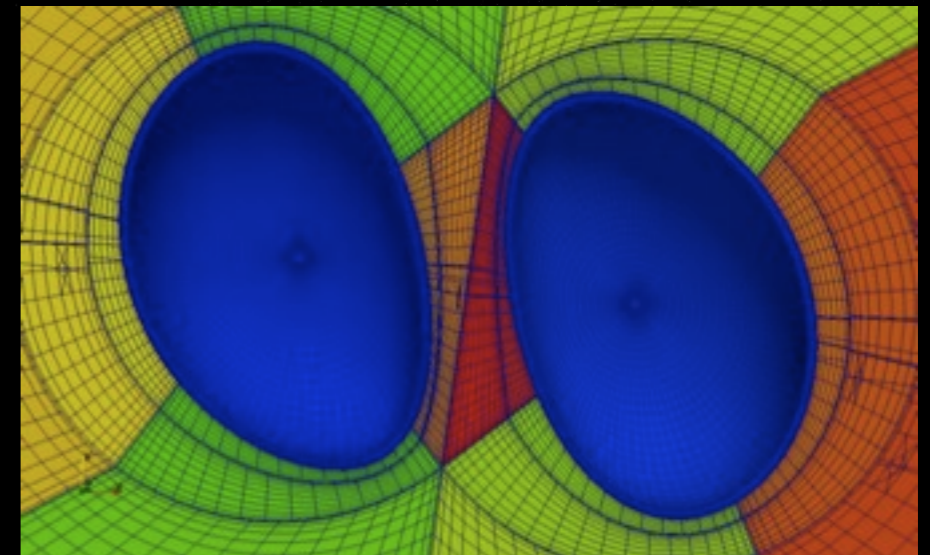
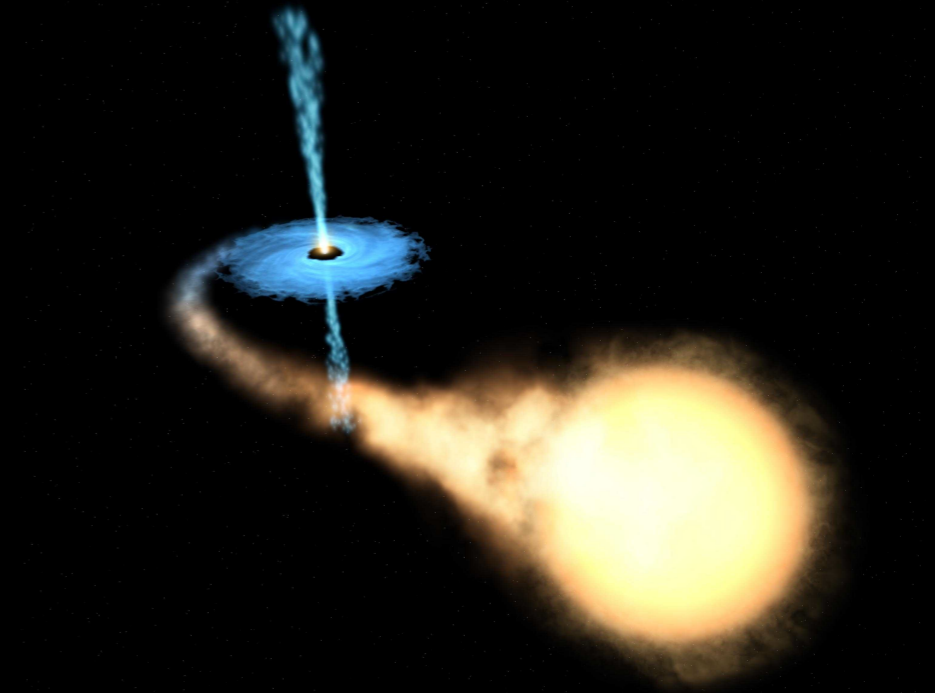
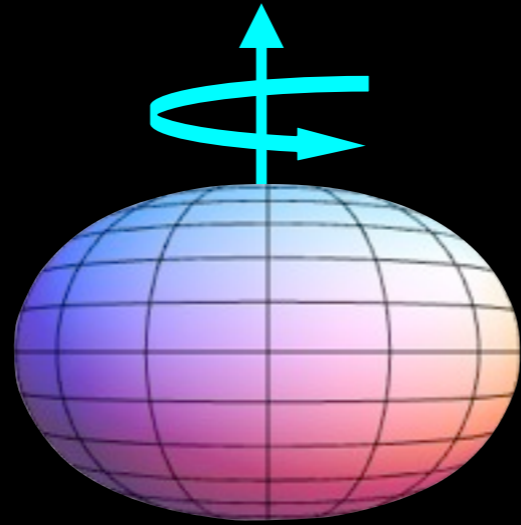
Mark A. Scheel & Béla Szilágyi (Caltech)

see also arXiv:1010.2771

May 21, 2011

Outline

- Black hole spin
- Motivation
 - Astrophysical
 - Physical
- Challenges
 - Initial data
 - Evolution
- Results
 - Black-hole eccentricity, spin
 - Gravitational waveforms
 - Horizon vorticity
 - Extremality & cosmic censorship



Black hole spin

- Dimensionless spin

$$\chi := \frac{S}{M^2} \quad \begin{array}{l} S = \text{spin angular} \\ \text{momentum} \\ M = \text{mass} \end{array}$$

- Geometrized units: $G = c = 1$

- Stationary black hole:

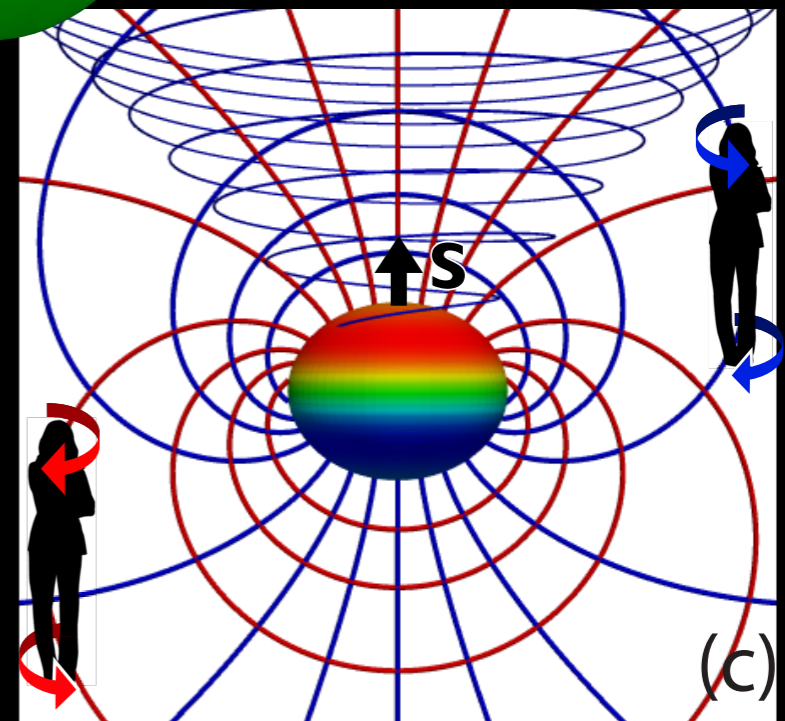
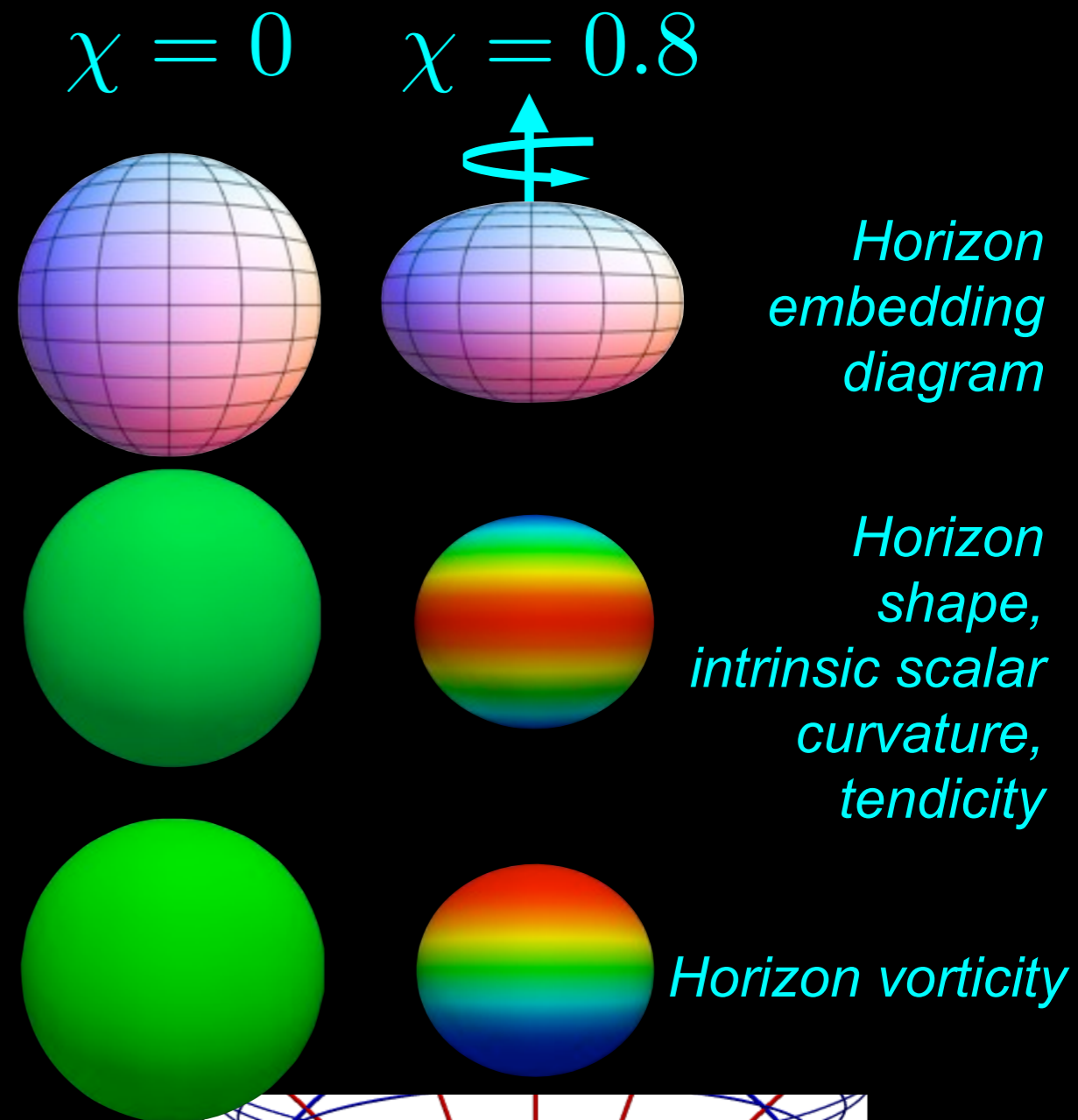
$$0 \leq \chi < 1$$

- Naked singularity if $\chi \geq 1$

- Spacetime geometry

- Nonspherical horizon

- Spacetime rotates: gyroscopes precess (“frame dragging”)



Introduction

- Astrophysical motivation

- Black holes could have spins $\chi := \frac{S}{M^2} \sim 1$

- Accretion models

- e.g. $\chi \sim 0.998$: neglect magnetohydrodynamics - K. S. Thorne (1974)*

- $\chi \sim 0.95$: include magnetohydrodynamics - S. L. Shapiro (2005)*

- Observational evidence (uncertain)

- e.g. microquasar GRS 1915+105*

- $\chi > 0.98$ - J.E. McClintock et al (2006)*

- $\chi \sim 0.7$ - M. Middleton et al (2006)*

- see also J. Blum et al (2009) & refs. therein*

- Predict gravitational waveforms from binary black holes (BBHs)

- Calibrate analytic waveform models

- Stellar-mass (ground detectors)

- Supermassive (space detectors)

- Final hole's mass, spin, recoil

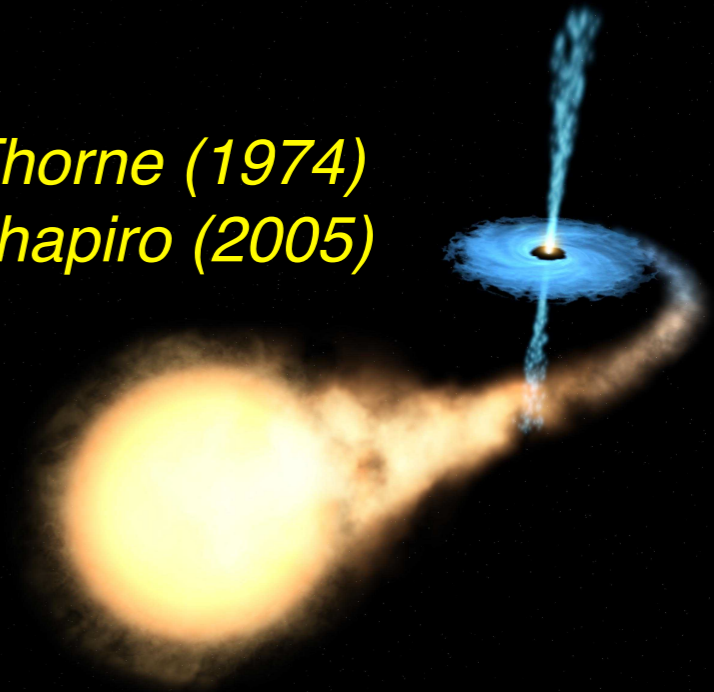


Image courtesy wikipedia



Image courtesy www.ligo.caltech.edu

Introduction

- Physical motivation

- Explore general relativity at its most extreme

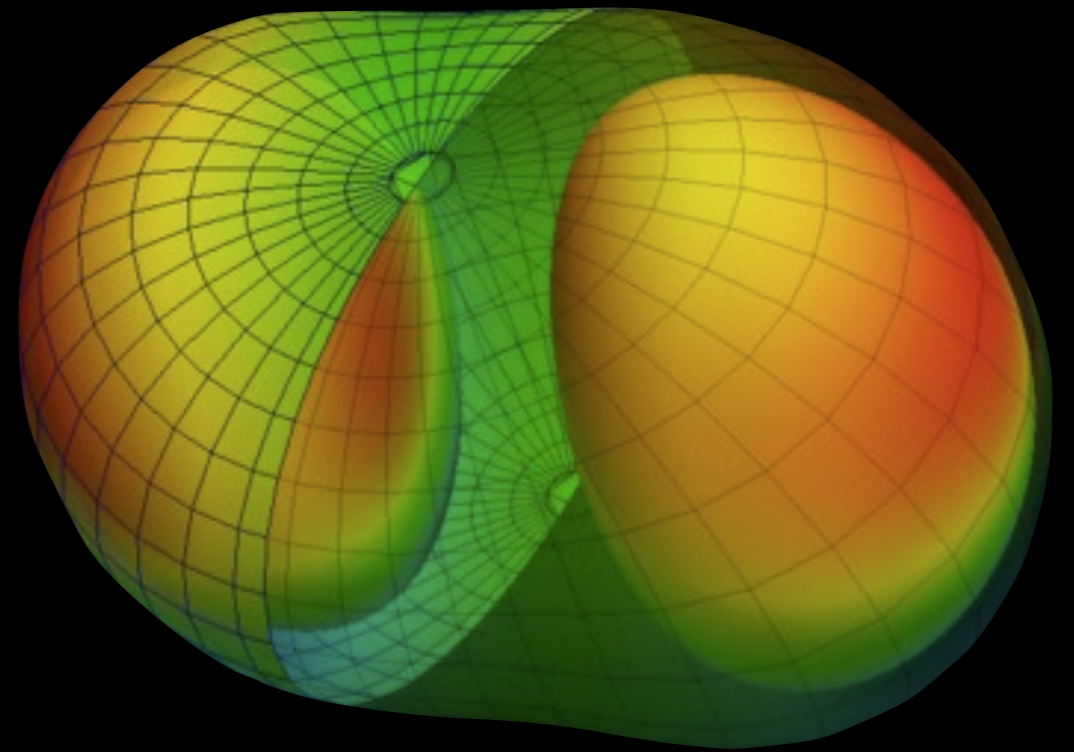
- Nonlinear behavior of strongly-warped spacetime

For details, see R. Owen et al (2011), cf. M. Scheel's talk this morning

- E.g. vorticity (“twisting”) and tendicity (“stretching/squeezing”) on and above horizon

- Extremality & cosmic censorship

- Stationary holes: naked singularity if $\chi \geq 1$
- Superextremal dynamical black holes?



Initial data

- Must satisfy constraints

Maxwell

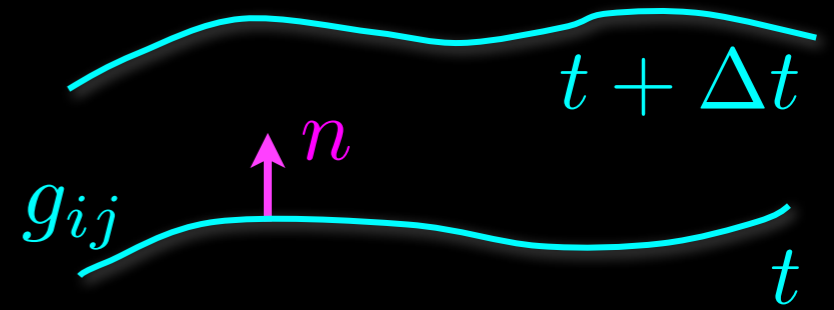
$$\nabla \cdot E = 0$$

$$\nabla \cdot B = 0$$

Einstein

$$G_{nn} = 0$$

$$G_{nj} = 0$$



–Conformally flat: $g_{ij} \propto f_{ij}$

- E.g. Bowen-York data: solve analytically $G_{nj} = 0$
J. M. Bowen (1979), J. M. Bowen & J. W. York, Jr. (1980)

- Can't make equilibrium spinning black holes
Garat & Price (2000)

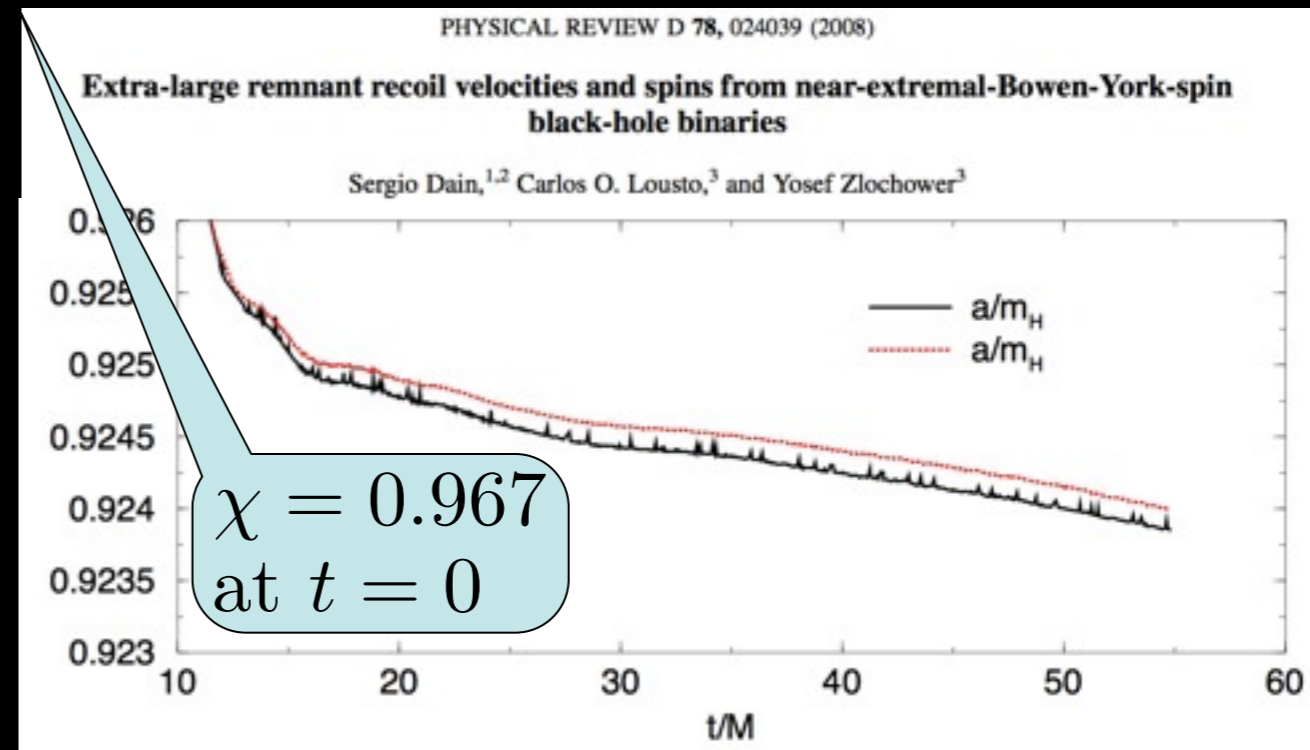
- Binaries: Spins $\chi < 0.93$

$$\chi = 0.8 \quad \text{L. Rezzolla et al (2008)}$$

$$\chi = 0.9 \quad \text{P. Marronetti et al (2008)}$$

$$\chi = 0.925 \quad \text{S. Dain, C. O. Lousto, \& Y. Zlochower (2008)}$$

$$\chi = 0.85 \quad \text{M. Hannam et al (2010)}$$



Initial data

- Must satisfy constraints

Maxwell

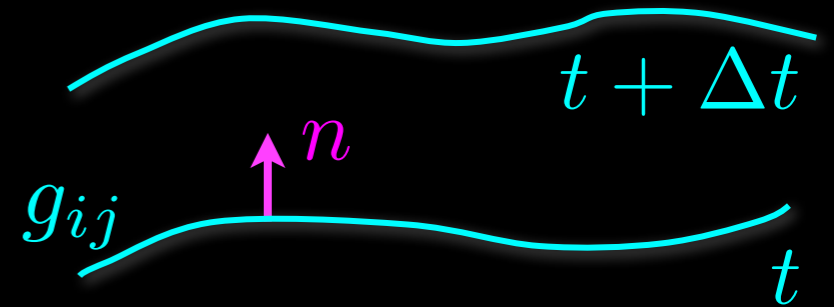
$$\nabla \cdot E = 0$$

$$\nabla \cdot B = 0$$

Einstein

$$G_{nn} = 0$$

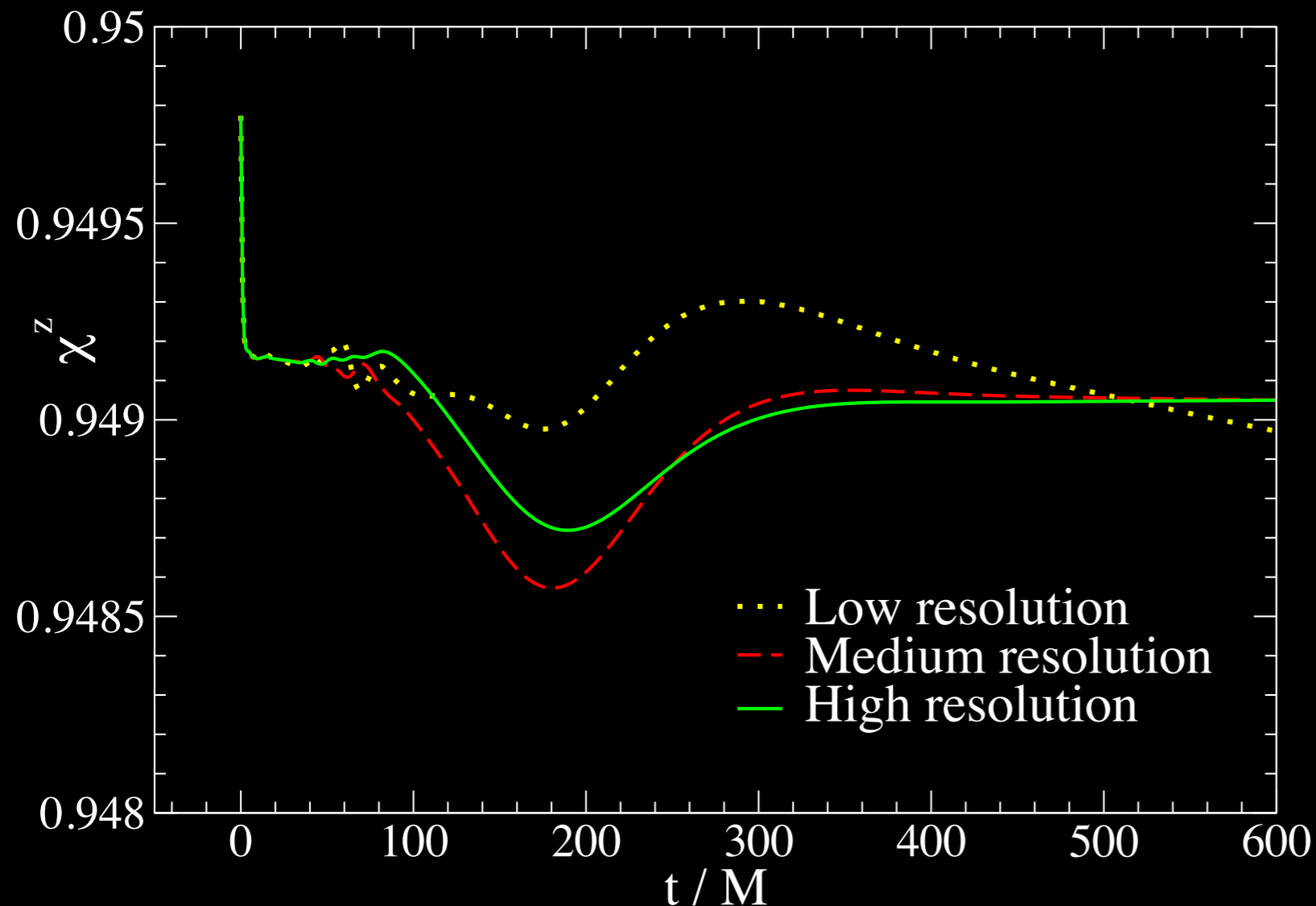
$$G_{nj} = 0$$



– Superposed-Kerr-Schild

GL, R. Owen, H. P. Pfeiffer, & T. Chu (2008)

- Must solve all (coupled) constraint equations



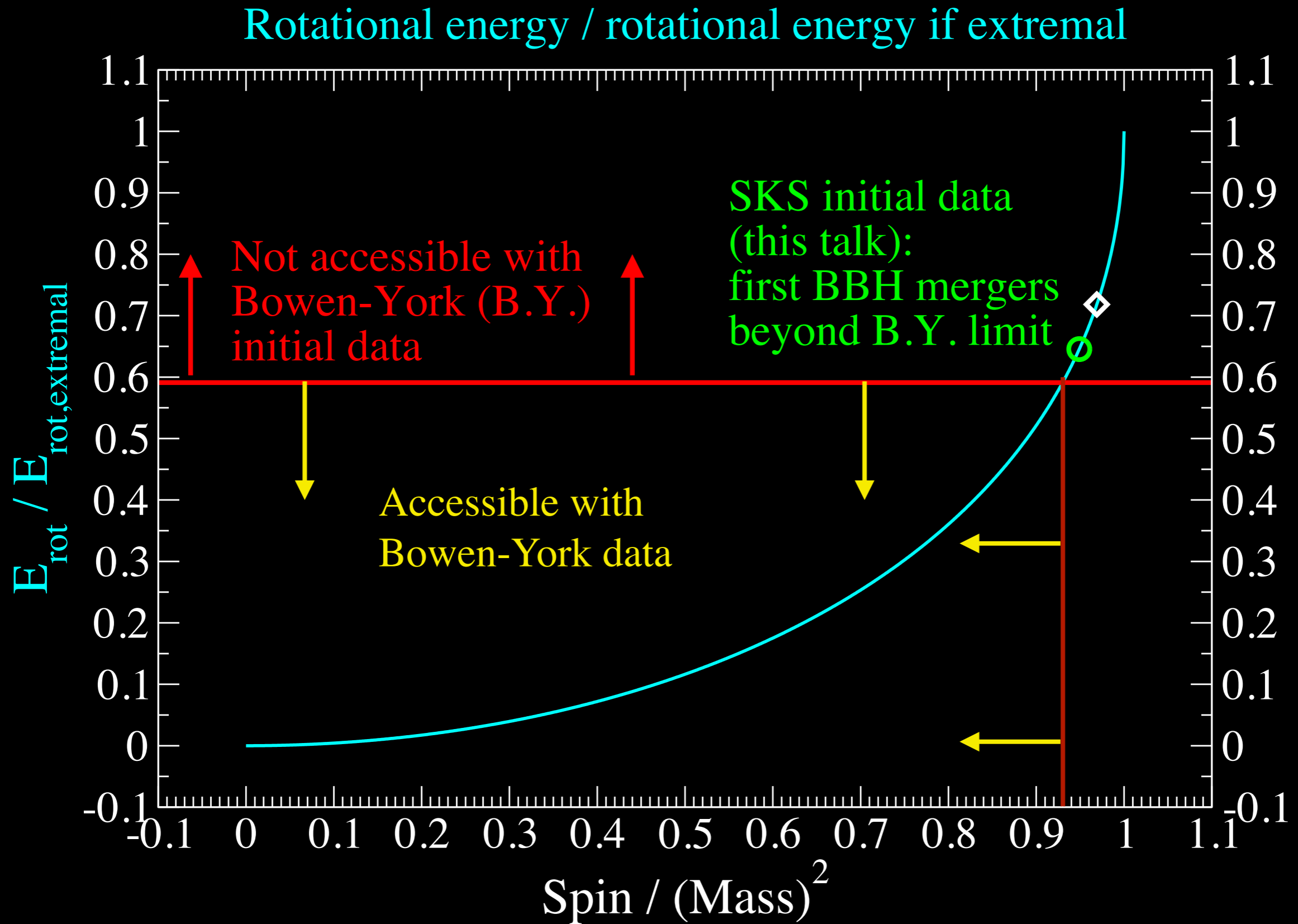
$$g_{ij} \propto f_{ij}$$

$$+ \sum_{n=1}^2 (h_{ij}^n - f_{ij}) e^{-r_n^2/w_n^2}$$

Metric of a boosted, spinning hole

Conformally flat except near horizons

Initial data



Evolution

- For high accuracy:
spectral methods
 - Require more resolution
near merger

use spectral adaptive mesh refinement

For details, cf. talk yesterday by B. Szilágyi

- Adjust resolution as needed
- Need smooth,
finite solution
 - Excise singularity
 - Grid coords. comove
with holes
 - Map between grid &
asymptotically
inertial coords.

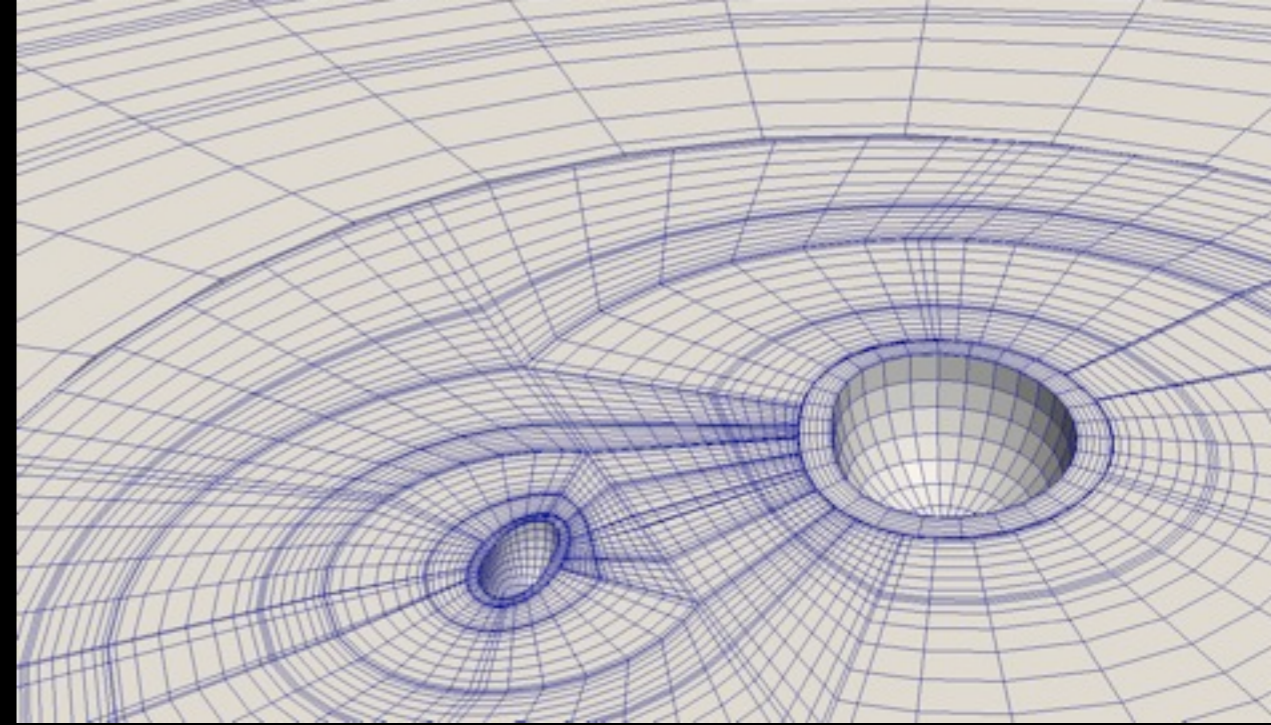
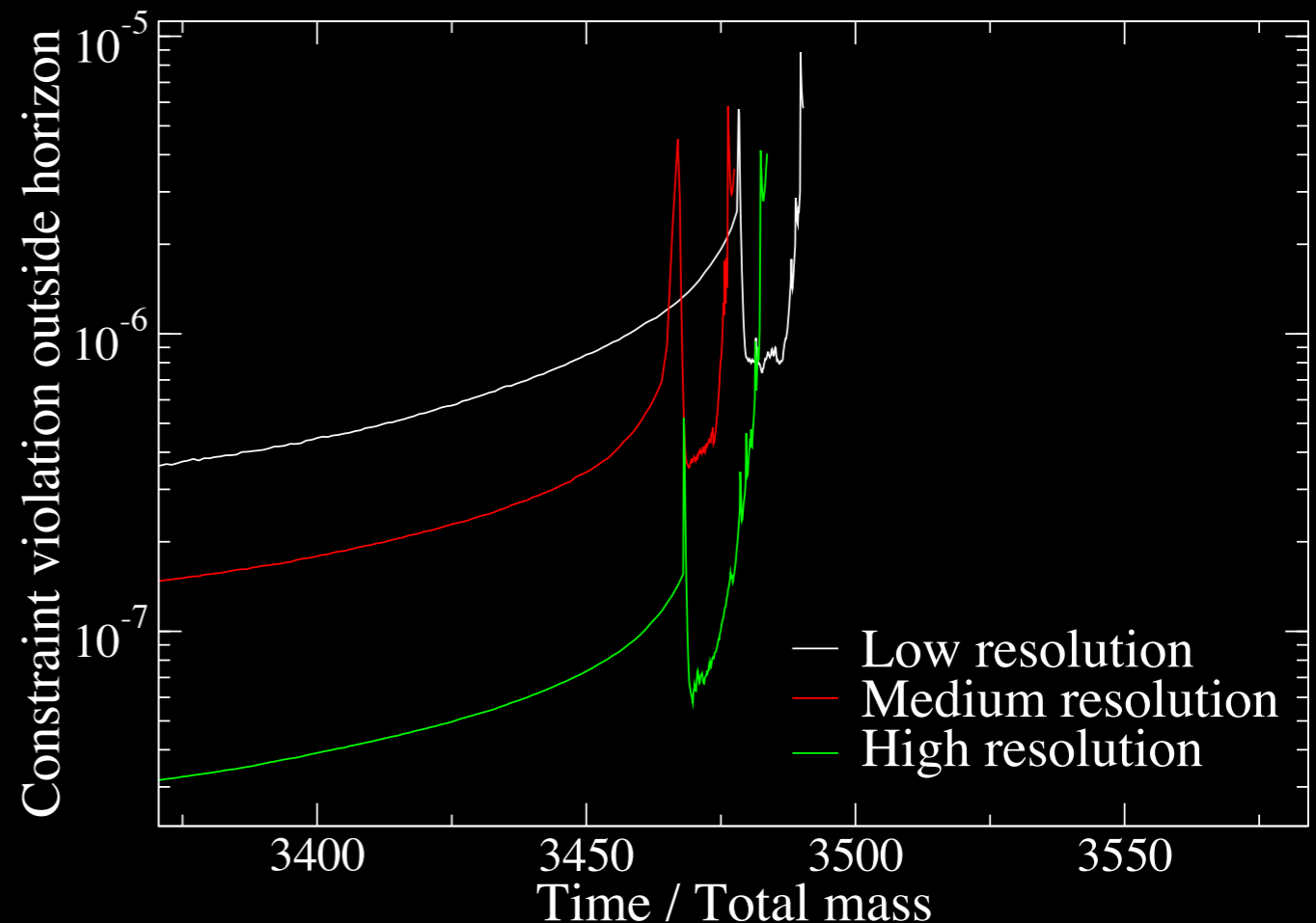


Figure courtesy Béla Szilágyi

Anti-aligned, equal mass BBH (spin=0.95)



Excision with high spins

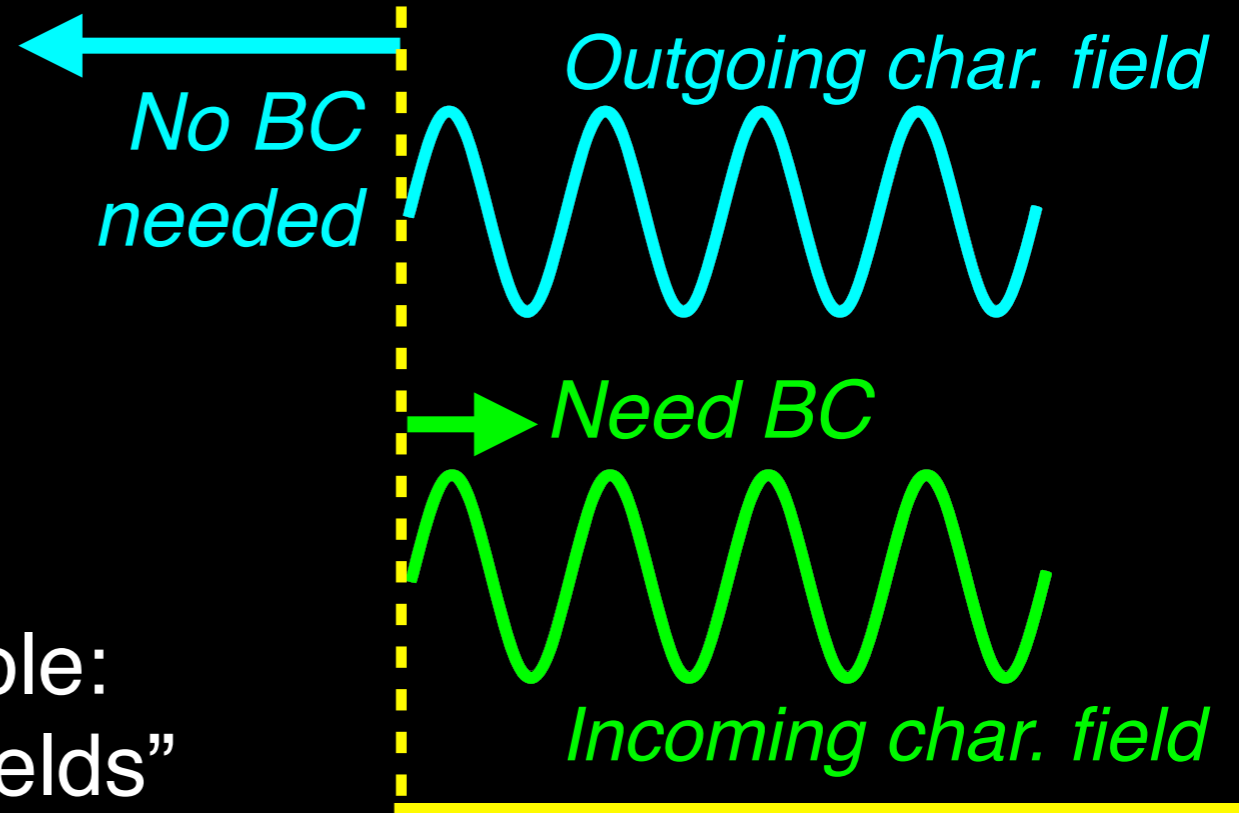
- Excision surface

- Must be inside horizon

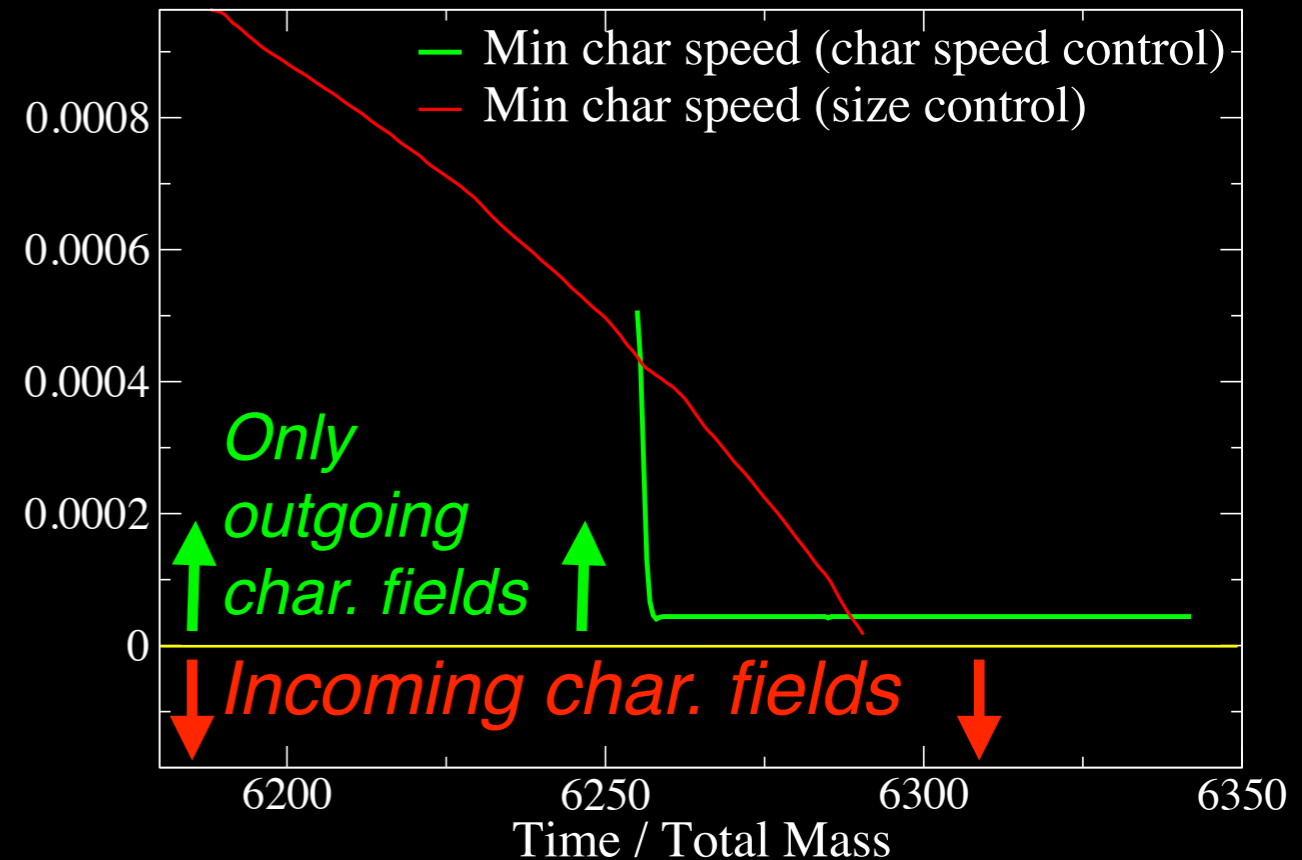
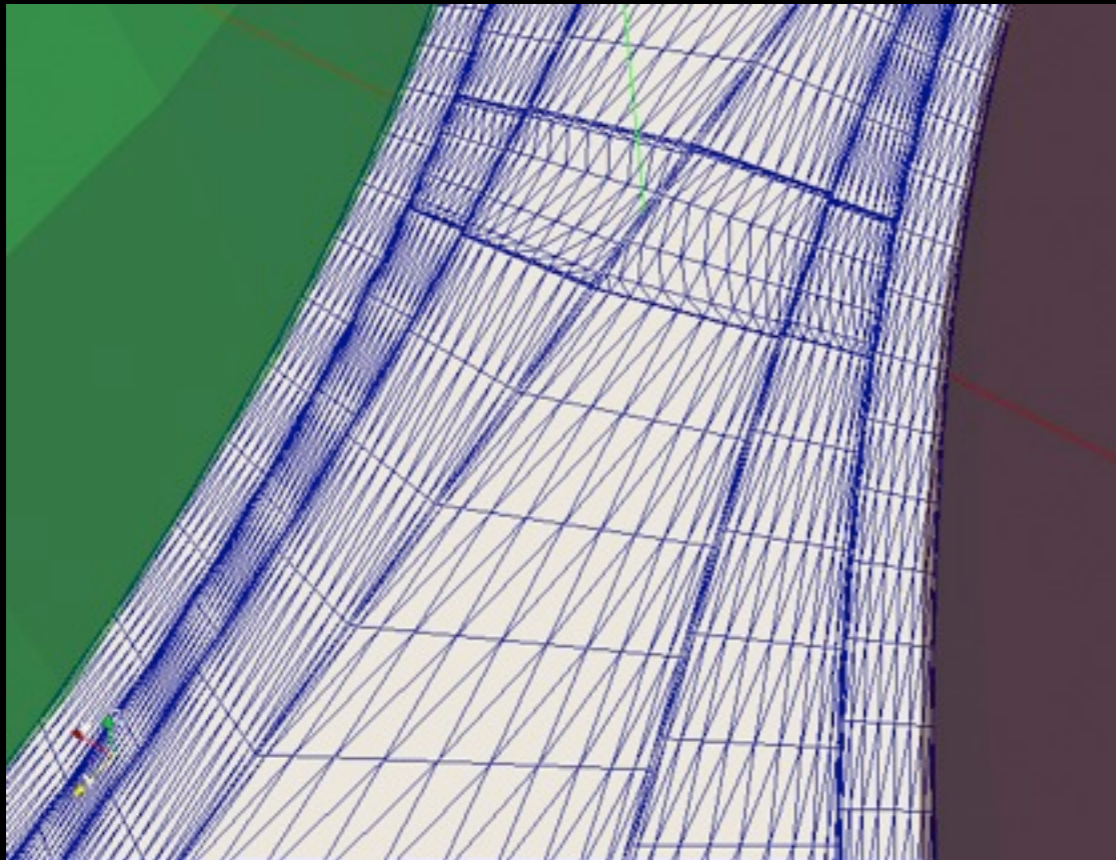
- No boundary condition (BC)

- OK if all info goes down the hole:
“only outgoing characteristic fields”

- Control excision surface shape, velocity



\mathcal{X}
E.g. wave equation



Results

$$\chi_A = \chi_B = -0.95\mathbf{e}_z$$

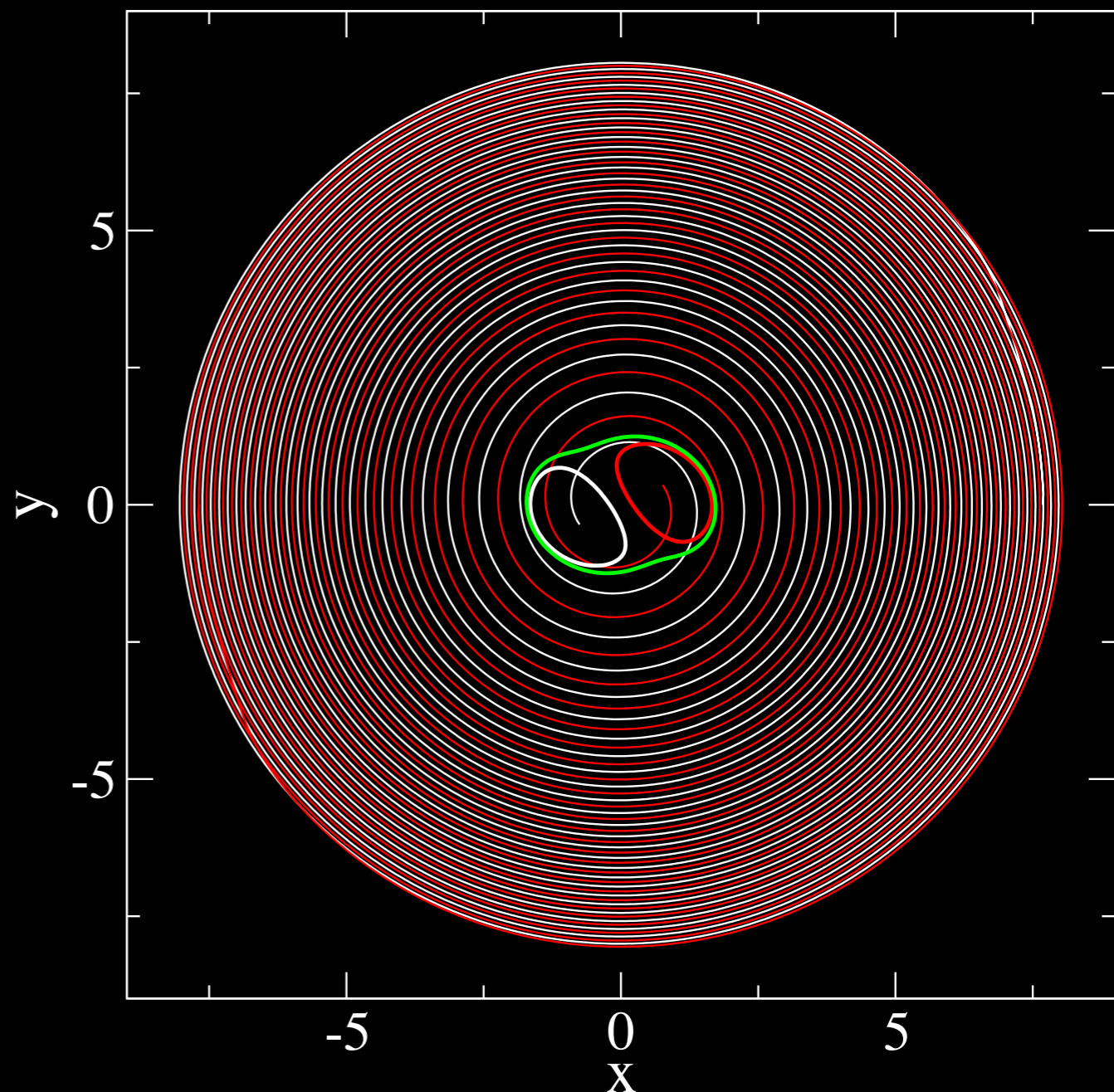
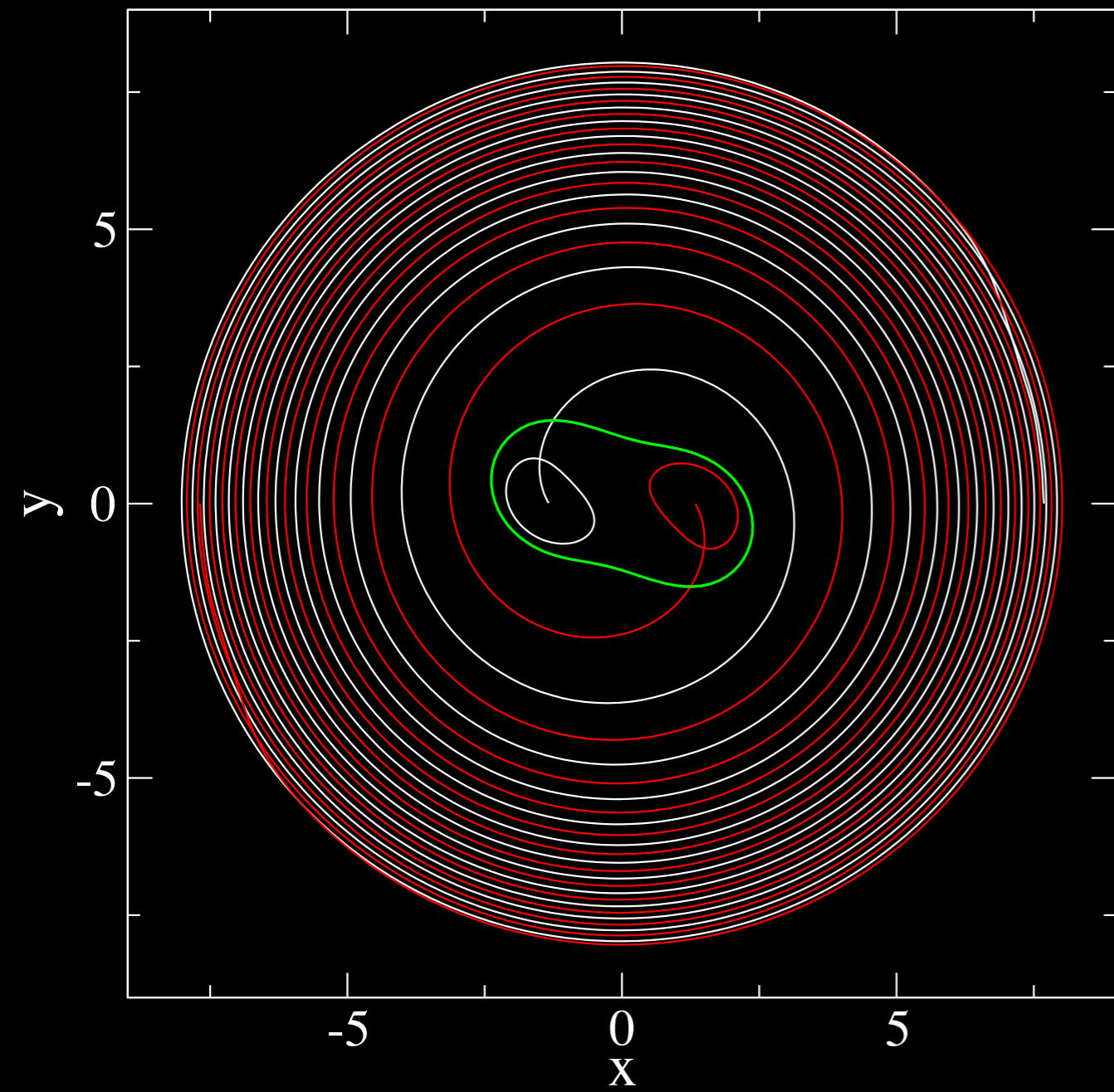
12.5 orbits

$$\chi_{\text{final}} = +0.3757$$

$$\chi_A = \chi_B = +0.97\mathbf{e}_z$$

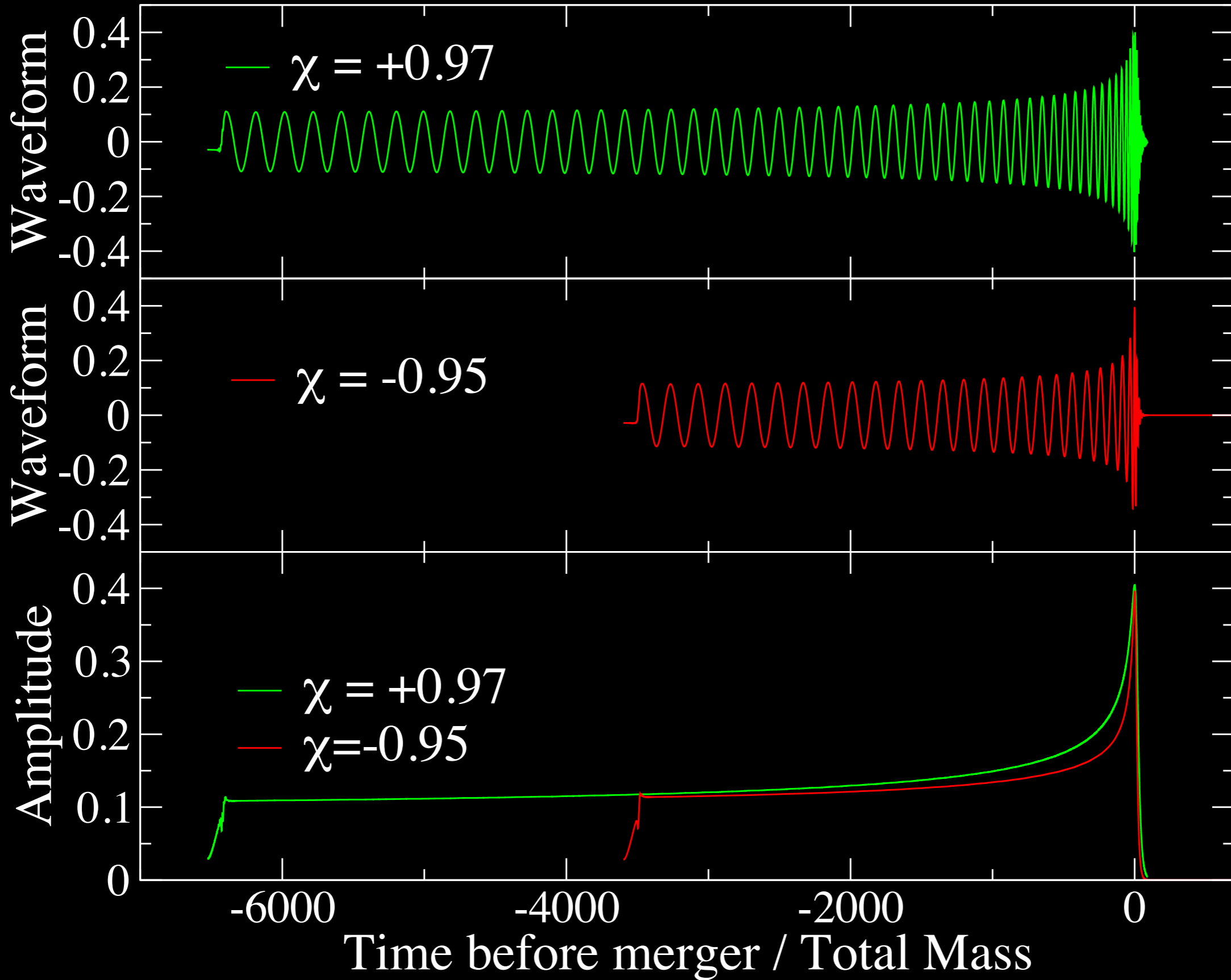
25.5 orbits

$$\chi_{\text{final}} \approx +0.945$$

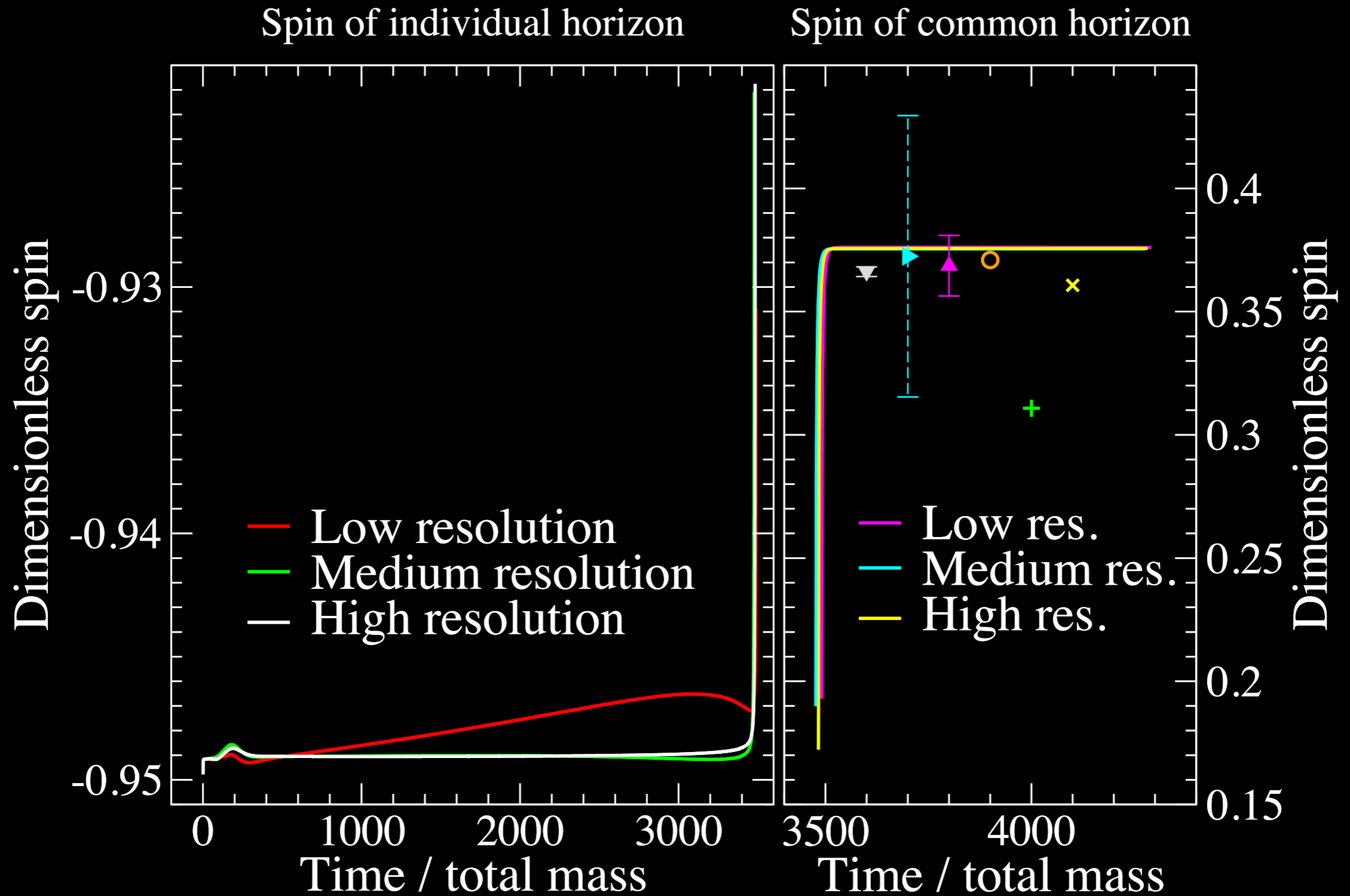


Waveforms

Real part of $(\ell, m) = (2, 2)$ mode
Waves extracted at radius $r/M = 100$



Spin vs. time



○ Campanelli, Lousto, and Zlochower (2006)

▶ Tichy and Marronetti (2008)

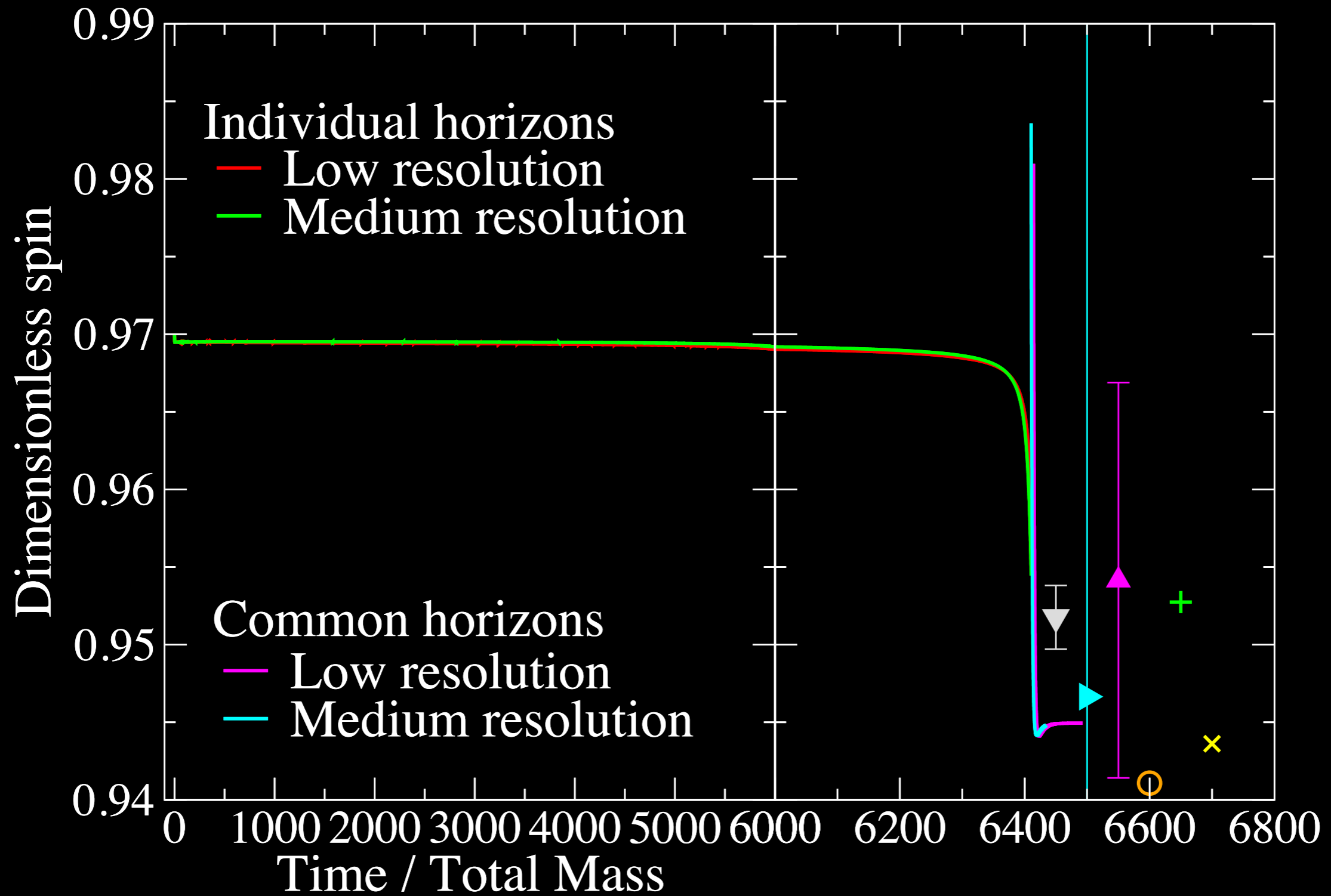
× Boyle and Kesden (2008)

▲ Barausse and Rezzolla (2009)

▼ Rezzolla *et al* (2008)

+ Buonanno, Kidder, and Lehner (2008)

Spin vs. time



○ Campanelli, Lousto, and Zlochower (2006)

▶ Tichy and Marronetti (2008)

× Boyle and Kesden (2008)

▲ Barausse and Rezzolla (2009)

▼ Rezzolla et al (2008)

+ Buonanno, Kidder, and Lehner (2008)

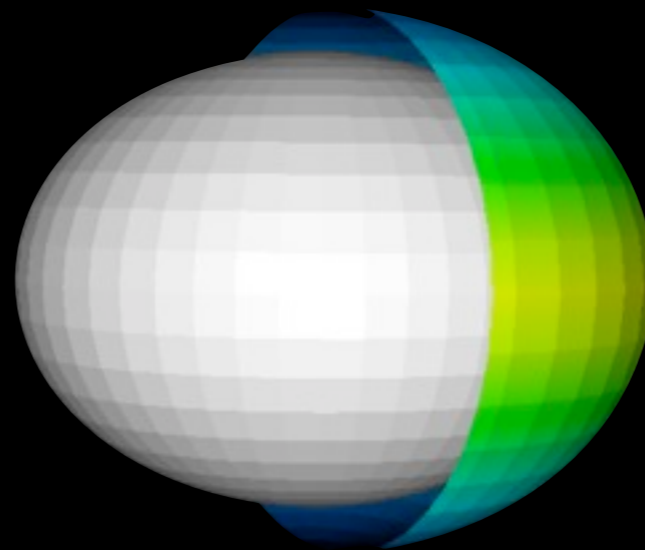
Extremality

- Initial data

$$\chi = S/M^2$$

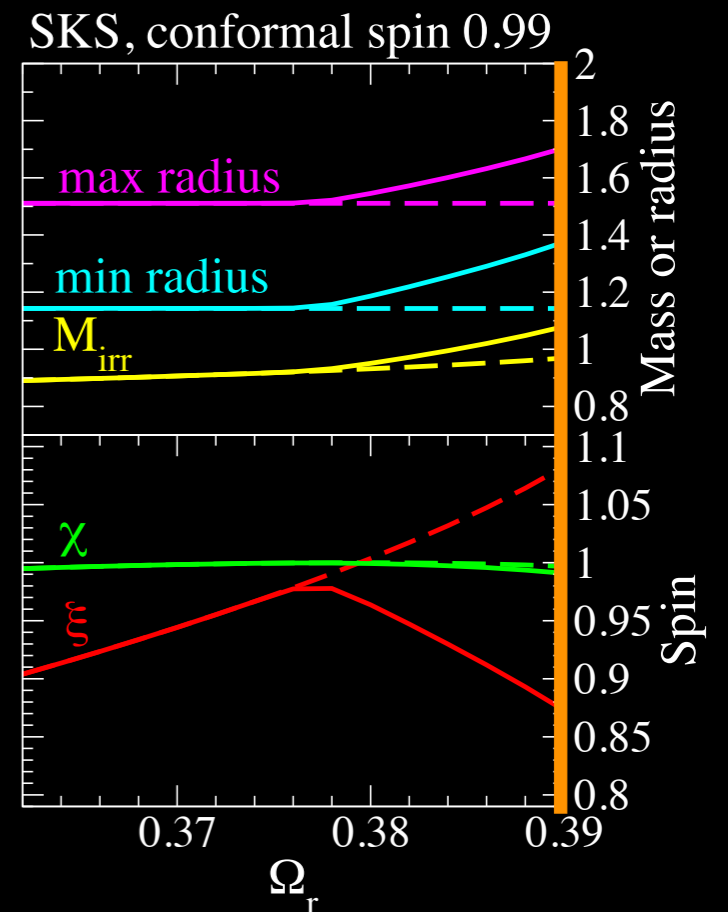
$$0 \leq \chi \leq 1$$

$$\xi = S/2M_{\text{irr}}^2$$



$$\Omega_r = 0.39$$

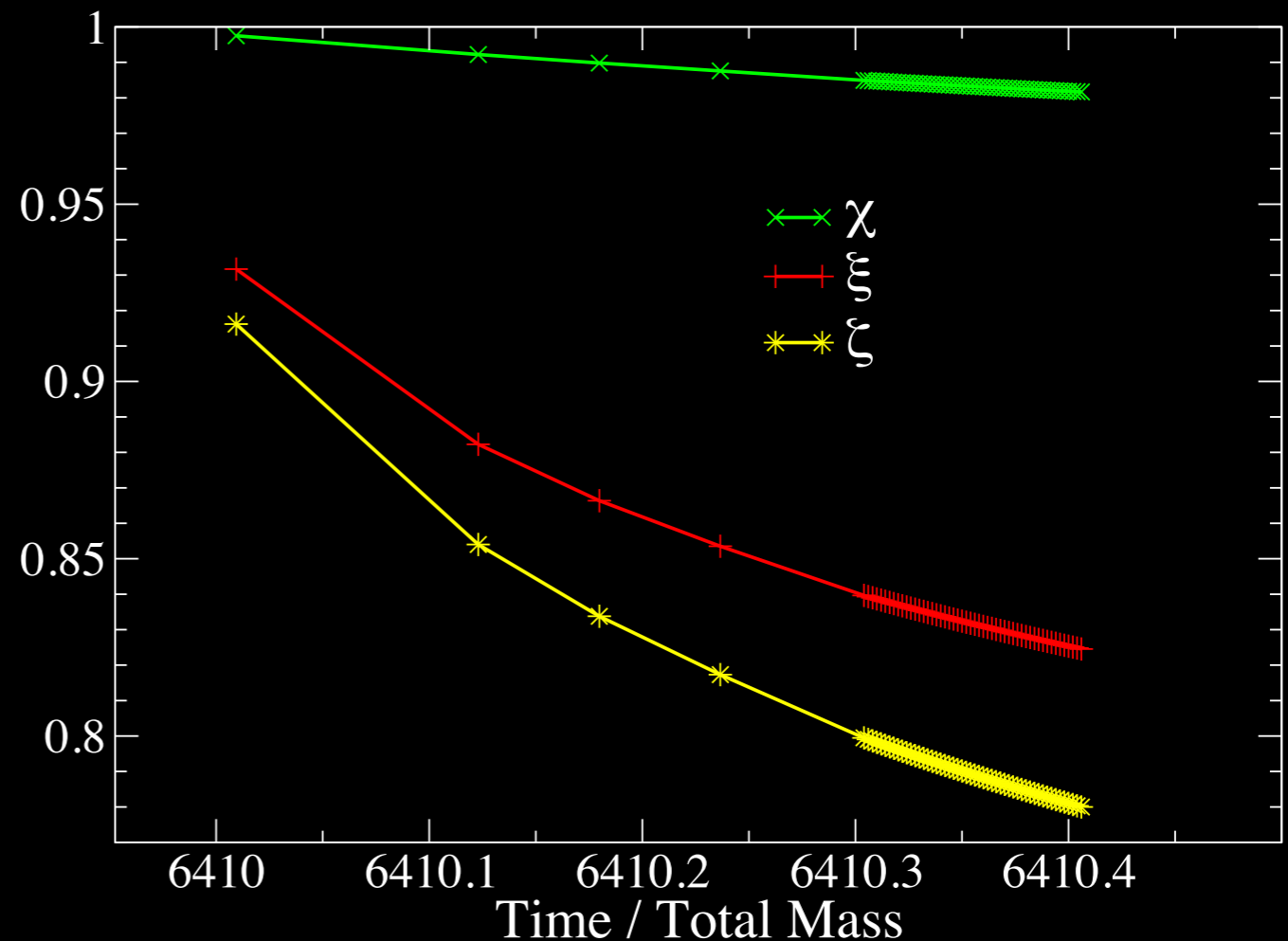
— Horizon - - Excision surface



- Evolution

$$\zeta = \frac{M_{\text{rot}}}{M_{\text{rot}}(\chi = 1)}$$

$$= \frac{1 - \sqrt{(1 + \sqrt{1 - \chi^2})/2}}{1 - 1/\sqrt{2}}$$

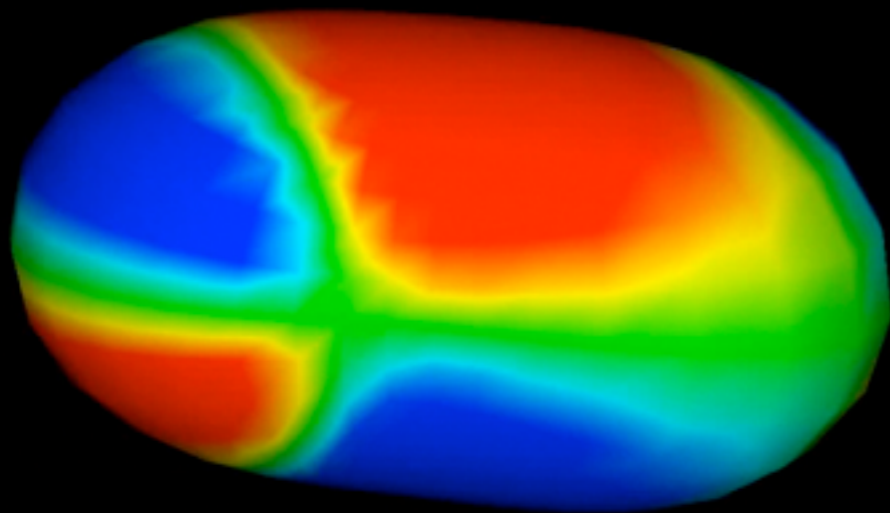


Horizon vorticity

$$\chi_A = \chi_B = -0.95\mathbf{e}_z$$

$$\chi_A = \chi_B = +0.97\mathbf{e}_z$$

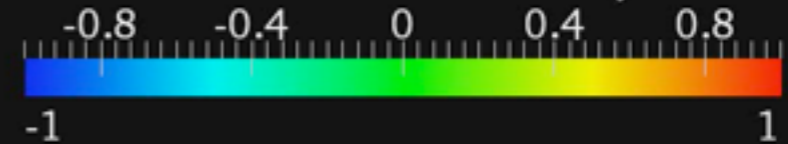
Rescaled for Ringdown



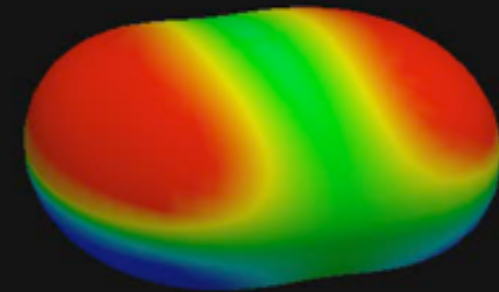
Time: 3483.0



Common horizon vorticity



(Paused to show common horizon)



Time: 6414.01

Movie courtesy Dave Kotfis

Conclusion

- Nearly extremal spins
 - Astrophysical black holes may have spins ~ 1
 - Improved initial data: can simulate BBH with spins beyond the Bowen-York limit of $\chi \lesssim 0.93$
 - This talk: spins up to $\chi = 0.97$

- Future work

- More simulations

- Unequal masses, generic spin direction

- Even higher spins

- Extract science from high-spin simulations

